Course Content

Unit 1: Sets, Real Number System and Logic Sete.

Sets and set operations, Theorems based on set operations.

Real Number System:

Real numbers. Field axioms. Order axioms. Interval. Absolute value. Geometrical representation of the real numbers.

Introduction, statements, Logical connectives, Truth tables, Basic laws of logic. Relations, Functions and Graphs

Relations:

Ordered pair, Cartesian product, Geometrical representation of Cartesian product, relation. Domain and range of a relation, Inverse of a relation.

Definition, Domain and range of a function, Functions defined as mappings, Inverse function, Composite function, functions of special type(Identity, Constant, Absolute and cubic), Trigonometric, Exponential logarithmic functions and their graphs.

Unit 3: Curve Sketching

Odd and even functions, Periodicity of a function, symmetry (about x - axis, y- axis and origin) of elementary functions, Monotonocity of a function, Sketching

 $\left(\frac{1}{x}, \frac{x^2 - a^2}{x - a}, \frac{1}{x + a}, x^2, x^3\right)$, Trigonometric, exponential, graphs of polynomial functions logarithmic functions (simple cases only)

Unit 4: Trigonometry

Inverse circular functions, Trigonometric equations and general values, properties of a triangle (sine law, Cosine law, tangent law, Projection laws, Half angle laws), the area of a triangle. Solution of a triangle (simple cases)

Unit 5: Sequence and Series, and Mathematical Induction

Sequence and Series:

Sequence and series, type of sequences and series (Arithmetic, Geometric, Harmonic),

Propertics of Arithmetic, Geometric, and Harmonic sequences, A.M., G.M. And H.M. Relation among A.M., G.M. and H.M., Sum of infinite geometric series. Mathematical Induction:

Sum of finite natural numbers. Sum of the squares of first n-natural numbers, Sum of cubes of first n - natural numbers. Intuition and induction, principle of mathematical induction.

Unit 6: Matrices and Determinants

Matrices and operation on matrices (Review), Transpose of a matrix and its properties, Minors and Cofactors, Adjoint, Inverse matrix. Determinant of a square matrix, properties of determinants (Without proof) upto 3×3 .

Unit 7: System of Linear Equations

Consistency of system of linear equations, solution of a system of linear equations by Cramer's rule, Matrix method (row - equivalent and Inverse) upto three variables.

Unit 8: Complex Number Definition of a complex number, Imaginary unit, Algebra of complex numbers, Geometric representation of a complex number, Conjugate and absolute value (Modulus) of a complex numbers and their properties, Square root of a complex number, Polar form of a complex number, product and Quotient of complex numbers. De Moivre's theorem and its application in finding the roots of a complex number.

properties of cube roots of unity. Unit 9: Polynomial Equations

Polynomial function and polynomial equations, Fundamental theorem of algebra (without proof), Quadratic equation Nature and roots of a quadratic equation, Relation between roots and coefficients, Formation of a quadratic equation, Symmetric roots. one or both roots common.

Unit 10: Co-ordinate Geometry

12 hrs

Straight line:

Review of various forms of equation of straight lines, Angle between two straight lines, condition for parallelism and perpendicularity, length of perpendicular from a given point to a given line, Bisectors of the angles between two straight lines.

[From unit 9]

Pair of lines: General equation of second degree in x and y, condition for representing a pair of lines, Homogeneous second degree equation in x and y, Angle between pair of lines, Bisectors of the angles between pair of lines. Unit 11: Circle Equation of a circle in various forms (Centre at origin, centre at any point, general equation of a circle, circle with a given diameter), Condition of Tangency of a line at a point to the circle, Tangent and normal to a circle. Unit 12: Limit and Continuity Limits of a function, Indeterminate forms, Algebraic properties of limits (without proof), Theorem on limits of algebraic, Trigonometric, Exponential and logarithmic $\lim_{x \to a} \frac{x^n - a^n}{x - a}, \lim_{x \to 0} \sin x \frac{\sin x}{x}, \lim_{x \to 0} \frac{e^x - 1}{x}, \lim_{x \to 0} \frac{\log(1 + x)}{x}$ Continuity of a function, Types of discontinuity, Graph of discontinuous function. Unit 13: The Derivatives Derivative of a function, Derivatives of algebraic, trigonometric, exponential and logarithmic functions by definition (simple forms), Rules of differentiation, Derivatives of parametric and implicit functions, Higher order derivatives. Unit 14: Applications of Derivatives Geometric interpretation of derivative, Monotonocity of a function, Interval of monotonocity, Extrema of a function, Concavity, Points of inflection, Derivative as Unit 15: Antiderivatives and its Applications Antiderivative, Integration using basic integrals, Integration by substitution and by parts method, the definite integral, The definite integral as an area under the given curve, Area between two curves. **Model Question** HSEB Examination 2071 (2014) Full Marks:- 100 Time: 3 hrs. Pass Marks:- 35 $5 \times 3 \times 2 = 30$ Group 'A' Define a statement. If p is true, q is true and r is true, find the turth value [From unit 1] of $(p \lor q) \land (\sim \lor)$. (Ans: False) For any two real numbers x and y, prove that: [From unit 1] $|x + y| \leq |x| + |y|$ Determine whether the function $f(x) = \sqrt{x^2-1}$ is even or odd. Also test its (c) [From unit 3] symmetricity. , (Ans: even function, symmetric about y-axis) [From unit 4.2] Solve for x: tan2x = tanx. (Ans: $x = n\pi$) Prove by mathematical induction: [From unit 5] $1 + 3 + 5 + \dots + n \text{ terms} = n^2$. 3 1 0 (c) Define singular matrix. Test whether the matrix if A = -2 1 -1 -1 3 -2 [From unit 6] singular or not. (Ans: Singular) Solve by 'nverse matrix method: [From unit 7] 2x + y = 7, x + 3y = 11. (Ans: x = 2, y = 3)Prove that the modulus of a complex number and its conjugate are [From unit 8] Find a quadratic equation whose roots are twice the roots of $4x^2 + 8x -$

> 5 = 0. (Ans: $x^2 + 4x - 5 = 0$)

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Find the obtuse of the line through (4, 2) which is parallel to
 4.
          (a)
                   x - 2y - 4 = 0.
                                                                                [From unit 10.1]
          (Ans: x - 2v = 0)
                   Find the equation of the circle which touches the axes at
                   (2, 0) and (0, 2).
                                                                                 [From unit 11]
          (Ans: x^2 + y^2 - 4x - 4y + 4 = 0)
                  Evaluate: \underset{X \to \infty}{\text{Lim}} (\sqrt{x+a} - \sqrt{x})
                                                                     (From unit 12.1)
         (Ans: 0)
                  Find \frac{dy}{dx} when x + y = \sin(x + y).
 5.
          (a)
                                                                                 [From unit 13]
                  Evaluate: \int \frac{\cos x - \sin x}{\cos x + \sin x} dx.
         (Ans: log(cosx + sinx) + C))
                  Find the intervals in which f(x) = x^2 - 2x + 10 is increasing or
                  decreasing.
         (Ans: Increasing on (1, ∞), decreasing on (-∞, 1))
                                           Group 'B'
                  For any three non-empty sets A, B, C, prove that:
         (a)
                 (A - B) - C = A - (B \cup C).
                                                                                  [From unit 1]
                 Define absolute value of a real number. Also, a is a positive real number
                 and x \in R then prove that:
                 |x| < a if and only if -a < x < a.
                                                                                  [From unit 1]
                 Sketch the graph of y = -x^2 + 4x - 3 indicating its characteristics.
        (b)
                                                                                  [From unit 3]
                 If \tan^{-1}x + \tan^{-1}y + \tan^{-1}z = \frac{\pi}{2}, show that: xy + yz + zx = 1.
7. (a)
                                                                                [From unit 4.1]
                 State sine law. Use this law to prove the projection law. [From unit 4.3]
                 Without expanding the determinant show that:
        (b)
                    1 a^2 a^3
                                     a^2 bc a
                      b^2
                          b^3
                                                                                 [From unit 6]
                                     c2 ab c | ab scient
                 Using Cramer's rule or row-equivalent method solve the following
        (a)
                x + y + z = 6, 2x + 3y + 5z = 23, 7x + 5y - 2z = 11
                                                                                 [From unit 7]
        (Ans: x = 1, y = 2, z = 3)
                If the roots of the equation x^2 + px + q = 0 are in the same ratio as these
        (b)
                of the equation x^2 + \ell x + m = 0, show that:
                p^2m = \ell^2a
                                                                                 [From unit 9]
                Prove that the tangents to the circle x^2 + y^2 = 5 at the point (1, -2) also
        (a)
                touches the circle x^2 + y^2 - 8x + 6y + 20 = 0
                                                                                [From unit 11]
        (b)
                Prove geometrically: \theta \rightarrow 0 \sin \theta = 0.
                                                                    [From unit 12.1]
                Show that the function
                                  when 0 \le x < \frac{1}{2}
                            when x = \frac{1}{2}
- x, when \frac{1}{2} < x < 1
                f(x) =
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is discontinuous at $x = \frac{1}{2}$

Also, redefine f(x) so as to f(x) be continuous at $x = \frac{1}{2}$. [From unit 12.2]

(a) Find, from definition, the derivative of $\sqrt{\frac{1}{1-x}}$. (Ans: $\frac{1}{2(1-x)}$)

(b) Using integration, find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.

[From unit 15.2] (Ans: πab)

Pir sa that for any positive real"D' quop le langues

Define inverse function. If $f:R \to R$ be defined by $f(x) = x^2 - 3$, find $f^{-1}(x)$. Also determine whether fof⁻¹ $(x) = f^{-1}$ of (x). [From unit 4.1] (Ans: $f^{-1}(x) = (x + 3)^{1/2}$)

Sum to n terms of the series: $\frac{2}{5} - \frac{6}{5^2} + \frac{10}{5^3} - \frac{14}{5^4} + \dots$ [From unit 5] $\left(\text{Ans: } \frac{1}{6} \left(1 + \frac{1}{5^{n-1}} \right) + \frac{(-1)^{n-1} (2n-1)}{3 \times 5^n} \right)$

Ans:
$$\frac{1}{6}\left(1+\frac{1}{5^{n-1}}\right)+\frac{(-1)^{n-1}(2n-1)}{3\times 5^n}$$

13. Find the angle between the pair of lines represented by a homogeneous equation of second degree. Also derive the condition of parallelism and perpendicularity of the lines. Find the angle between the lines represented by $x^2 + 9xy + 14y^2 = 0$

Ans: θ : $\tan^{-1}\left(\pm \frac{2\sqrt{h^2 - ab}}{a + b}\right)$

Condition of Perpendicularity: a + b = 0

Condition of parallelism: h2 = ab)

Find the bisectors of the angles between the lines $\ell_1x + m_1y + n_1 = 0$ and $\ell_2 x + m_2 y + n_2 = 0$. Also determine the condition that the bisector of the angle in [From unit 10.1] which the origin lies.

$$\frac{\ell_1 x + m_1 y + n_1}{\sqrt{\ell_1^2 + m_1^2}} = \pm \frac{\ell_2 x + m_2 y + n_2}{\sqrt{\ell_2^2 + m_2^2}}$$
Ans:
$$\frac{\ell_1 x + m_1 y + n_1}{\sqrt{\ell_1^2 + m_1^2}} = \pm \frac{\ell_2 x + m_2 y + n_2}{\sqrt{\ell_2^2 + m_2^2}}$$

State De Moivre's theorem. Using De Moivre's theorem find the square roots of $4 + 4\sqrt{3}i$ [From unit 8]

(Ans: ± (√6+i√2)) Toomos s to standard India vinawi to ci

A window is the form of a rectangle surmounted by a semi circle. If the total perimeter is 9m, find the radius of the semicircle for the greatest window's area. vine laced one vine shipM deset vindFrom unit 14.2]

$$\left(\text{Ans:} \frac{9}{4+\pi} \text{m}\right)$$

Water flows into an inverted conical tank at the rate of 42cm3/sec. When the depth of the water is 8cm, how fast is the level rising? Assume that the height [From unit 14.3] of the tank is 12 cm and the radius of the top is 6cm.

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Ans: 21 cm/sec

Exam Questions

Unit I - Sets, Real Number System and Logic

If $A = \{a, e, i\}$, $B = \{e, u\}$, $U = \{a, e, i, o, u\}$, find $A \cup B$ and $A \cap B$. [Q.N.1(a), 2056] (Ans: {0} and {a, i, o, u}) Rewrite, without using absolute value sign for |3x + 2| <1. 2. [Q.N.1(b), 2056]

Ans: $-1 \le x \le$

3. Define the union and the intersection of two sets. If A , B and C are subsets of U, prove $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ [Q.N.7(a), 2056] Prove that for any positive real number $a_1|x| < a$ implies -a < x < a.

[Q.N.1(a), 2057] Define the complement of a set. State and prove De-Morgan's laws. [Q.N.7(a), 2057]

6. If $U = \{1, 2, \dots, 10\}$, $A = \{x : x \ge 4\}$, $B = \{x : x < 8\}, \text{ find } A \cap B \& A - B.$ [Q.N.1(a), 2058] (Ans: {4, 5, 6, 7} and {8, 9, 10}) 7.

If A, B, C are subsets of a universal set U, prove that,

 $A - (B \cap C) = (A - B) \cup (A - C)$ [Q.N.7(a), 2058] If $A = \{a, e, i, o u\}$ and $B = \{a, b, c, d, e\}$ are two given sets, find $A \cup B$ and A - B.

(Ans: {a, b, c, d, e, i, o, u} and {i, o, u})

[Q.N.1(a), 2059]
In a certain village in Nepal, all the people speak Nepali or Tharu or both languages. If 90% speak Nepali and 20% Tharu language, how many speak

(i) Nepali only (ii) Tharu language only and (iii) both languages. [Q.N.7(a), 2059] Persons speaking Nepali only = 80% Ans: Persons speaking Tharu only = 10% Persons speaking both languages = 10%

10. If $O = \{1, 3, 5, 7, 9\}$ and $P = \{2, 3, 5, 7\}$, find $O \cap P$ and P = O with the help of Venn diagram. [Q.N.1(a), 2060]

(Ans: $O \cap P = \{3, 5, 7\}$ and $P - O = \{2\}$)

- 11. In a group of students 24 study Maths, 30 study Biology, 22 study physics; 8 study Maths only, 14 study Biology only, 6 study Biology and Physics only, and 2 study Maths and Biology only. Find:
- (i) how many study all three subjects.

(ii) how many students were in the group. (Ans: (i) 8 (ii) 46)

[Q.N.7(a), 2060]

[Q.N.1(a), 2061]

12. If $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ be the universal set and $M = \{1, 3, 5, 7\}$,

 $N = \{2, 4, 6, 8\}$, then find $M \cup N$ and $M \cap N$.

(Ans: $\overline{M \cup N} = \{9\}$ and $\overline{M \cap N} = \{1,2,3,4,5,6,7,8,9\}$) In a group of twenty eight teachers of a school, 15 teach English, 15 teach 13. Maths, 14 teach Nepali, 7 teach English and Maths, 6 teach English and Nepali, 5 teach Maths and Nepali. Find how many teach all three subjects, how many teach Maths only and Nepali only. [Q.N.7(a), 2061] (Ans: $n(E \cap M \cap N) = 2$, $n_0(M) = 5$ and $n_0(N) = 5$)

14. If $A = \{1, 3, 5, 7\} \& B = \{2, 3, 5\}$, find $A \cap B$ and A - B. Show them in Venndiagram. [Q.N.1(a), 2062] (Ans: $A \cap B = \{3, 5\}$ and $A - B = \{1, 7\}$)

Define Union and Intersection of two sets. Illustrate them through Venndiagrams. Let A, B, C be any non-empty subsets of U, prove that: $A \cup (B \cap C) = (A \cup B) \cap (A \cup C).$ [Q.N.7(a), 2062]

- 16. $A = \{x : x = 2n+1, n \le 6, n \in \mathbb{N}\}, B = \{x : x = 3n-2, n \le 3, n \in \mathbb{N}\}$ Write the following by using the modulus sign: $-1 \le x \le 5$ 17. [Q.N.3(c), 2063] $(Ans: |x-2| \leq 3)$ Of the number of three athletic teams, 21 are in the basketball team, 26 in hockey 18. team and 29 in football team, 14 play hockey and basketball, 15 play hockey and football, 12 play football and basketball, and 8 play all the games. How many members are there in all? [Q.N.7(a), 2063] (Ans: 43) 19. Find A ∪ B if : $A = \{x : x = 2n+1, n \le 5, n \in N\}$ $B = \{x : x = 3n-2, n \le 4, n \in N\}$ [Q.N. 1(a), 2064] (Ans: {1, 3, 4, 5, 7, 9, 10, 11}) [Q.N. 3(c), 2064] Write [x-7] < 3 without using the modulus sign. 20. (Ans: 4 < x < 10)A village has total population 25,000 out of which 13,000 read 'Gorkhaptra' and 21. 10,500 read 'Kantipur' and 2500 read both papers. Find the percentage of population who read neither of these papers. [Q.N. 7(a), 2064] (Ans: 16%) 22. Given A = [-2, 4] and B = (2, 5], compute $A \cup B$ and $A \cap B$. [Q.N. 1(a), 2065] (Ans: [-2,5], [2,4]) 23. Out of a group of 20 teachers in a school, 10 teach Maths, 9 teach Physics, 7 teach Chemistry, 4 teach Maths and Physics, but none teach both Maths and Chemistry: How many teach Physics and Chemistry? How many teach only Physics? (iii) How many teach only Chemistry? [Q.N. 7(a), 2065] (Ans: (i) 2 (ii) 3 (iii) 5) 24. Given $A = \{1, 2, 3\}$ and $B = \{3, 4, 5, 6\}$, show that $A - (A - B) = A \cap B$. [Q.N.1 (a), 2066] 25. Twenty three medals are awarded for folksongs, eight for Deuda songs and eleven for Maithili songs. If the total number of singers awarded is thirty two and only three singers received medals in all three types of songs, find how many singers received medals in exactly two of three types of songs. (Ans: 4) [Q.N.7 (a), 2066] Define Power set. Write the power set of the set A {a, b, c}. 26. 2 [Q.N. 1 (a), 2067] (Ans: {φ, {a}, {b}, {c}, {a, b}, {b, c}, {c, a}, {a, b, c}} In a group of students 30 study maths, 24 study physics, 22 study chemistry, 14 study maths only, 8 study physics only, 6 study maths and chemistry only, 2 study maths and physics only and 8 study none. How many students are in the group? How many study chemistry only? How many study all three subjects? (Ans: 60, 2, 8) 4 [Q.N.7 (a), 2067] 28. Define disjunction of two statements. Prepare a truth table for the compound statement $\sim (p \ v \ q)$ [Q.N.1(a),2068] Let $A = \{1,2,3,4\}$ and $B = \{1,3,5\}$. Find the relation R from Set A to Set B determined by the condition x > y. (Ans: {(2, 1), (3, 1), (4, 1), (4, 3)} [Q.N.1(b),2068] If A, B and C be any three non-empty sets, Prove that: $A - (B \cup C) = (A - B) \cap (A - C)$. [Q.N.6(a),2068] 31. Define absolute value of a real number. Rewrite the following relation without
 - using absolute value sign \times \times 1 vino one is a set of the event and $|2x-1| \le 5$. (x) is a new |x| = 31 = -101 = 81 the negative as Also, draw the graph of the inequality. [Q.N.6(a)(Or),2068]

170 ... Class XI (Humanities) : Chapter-wise Question Collection with Syllabus 32. Define negation of a statement. Construct a truth table for the compound [Q.N. 1(a), Set 'A' 2069] statement $\sim (pv(\sim q))$. 33. Define union and intersection of two sets. If A, B and C are any three nonempty sets, prove that: $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$. [Q.N. 6(a), Set 'A' 2069] 34. If $x \in R$ and a is any positive real number, Prove that: $|x| < a \implies -a < x < a$ and conversely. [Q.N. 6(a)(Or), Set 'A' 2069] 35. Write inverse and converse of the statement 'if 3 is an odd number then 6 is not an odd number'. [Q.N. 1(a), Set 'B' 2069] 36. Define De-Morgan's law. For any non-empty sets, A, B, C prove: $A - (B \cup C) = (A - B) \cap (A - C)$. [Q.N. 6(a), Set 'B' 2069] Define absolute value of a real number. For any two real numbers x and y 37. prove that: $|x + y| \le |x| + |y|$. [Q.N. 6(a)(Or), Set 'B' 2069] 38. Define disjunction of two functions. Construct a truth table for the compound statement. (~p) v (~q). [Q.N. 1(a), Supp. 2069] 39. Let $A = \{a, b\}$, $B = \{b, c\}$ and $C = \{c, d\}$. Find $A \times (B \cup C)$ and $A \times (B \cap C)$. [Q.N. 1(b), Supp. 2069] (Ans: {(a, b), (a, c), (a, d), (b, b), (b, c), (b, d)}, {(a, c), (b, c)}) 40. If A, B and C are any three non-empty sets, prove that: $A - (B \cap C) = (A - B) \cup (A - C)$ [Q.N. 6(a), Supp. 2069] 41. Prepare a truth table for the compound statement P v ~ (pAq). What would you conclude from the truth table? [Q.N. 1(a), 2070 'C'] 42. Let A = {1, 2, 3, 4}. Find the relation on Asatisfying the condition x+y≤4. (Ans: {(1, 1), (1, 2), (1, 3), (2, 1), (2, 2), (3, 1)}) [Q.N. 1(b), 2070 'C'] 43. Define union and intersection of two sets. If A, B and C are any three nonempty sets, prove that: , [Q.N. 6(a), 2070 'C'] $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$. (Ans: $A \cup B = [-3, 4], A \cap B = [-2, 1], A - B = [-3, -2), B - A = (1, 4])$ Let A = [-3, 1] and B = [-2, 4]. Find $A \cup B$, $A \cap B$, A - B and B - A. 44. {Ans: [-3, 4], [-2, 1], [-3, -4), (1, 4]} [Q.N. 6(a)(Or), 2070 'C'] 45. If p and q are any two statements, prove that: $p \vee q \equiv q \vee p$. [Q.N. 1(a), 2070 'D'] Let $A = \{a, b\}, B = \{b, c\} \text{ and } C = \{c, d\}. \text{ Find : }$ 46. $A \times (B \cup C)$ and $A \times (B \cap C)$. [Q.N. 1(b), 2070 'D'] (Ans: {(a, b), (a, c), (a, d), (b, b), (b, c), (b, d)}, {(a, c), (b, c)}} 47. Define union and intersection of two sets. If A, B and C are any three nonempty sets, prove that: Q.N. 6(a), 2070 'D'] $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$. Define a statement. If p is true, q is true and r is true, find the turth value of [Q.N. 1(a), 2071 'C'] (p∨q) ∧ (~ ∨). (Ans: False) 49. For any two real numbers x and y, prove that: [Q.N. 1(b), 2071 'C'] $|x+y| \leq |x| + |y|$ 50. For any three non-empty sets A, B, C, prove that: $(A - B) - C = A - (B \cup C)$. [Q.N. 6(a), 2071 'C'] Define absolute value of a real number. Also, a is a positive real number and 51. $x \in R$ then prove that: |x| < a if and only if -a < x < a. [Q.N. 6(a)(Or), 2071 'C'] [Q.N. 1(a), 2071 'D'] 52. Construct truth table of ~(p\vq). For any two real numbers x and y, prove that: 53. [Q.N. 1(b), 2071 'D'] $|x-y| \ge |x|-|y|$. [Q.N. 6(a), 2071 'D'] 54. Prove that: $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$. Define absolute value of a real number. If a is a positive real number and $x \in \mathbb{R}$, 55. then prove that: |x| < a if and only if -a < x < a. [Q.N. 6(a)(Or), 2071 'D']

56.

Prove that the function f: IR – {3} \rightarrow IR – {1} given by f(x) = $\frac{X}{x-3}$ is bijective. [Q.N. 11, 2071 'D']

Unit 2 - Relations, Functions and Graphs

- 1. Let $f: R \rightarrow R$ and $g: R \rightarrow R$ be defined by $f(x) = x^2 + 1$; $g(x) = x^5$ find f^{-1} ; (gof) (x) and (fog) (x).

 (Ans: $(x-1)^{1/2}$, $(x^2+1)^5$ and $x^{10}+1$)
- 2. When does a function $f: A \rightarrow B$ become an onto and one to one ? [Q.N.1(b), 2057]
- 3. A function f(x) is defined as follows: $f(x) = 4x - 2 \text{ for } x \ge 1 \\ \text{for } x \le 1 \end{cases}, \text{ find } f(2); f(1); f(0); f(-1); \frac{f(h) - f(1)}{h} \text{ for } 1 \le h.$

[Q.N.7(b), 2057]

Ans: f(2) = 6, f(1) = 2, f(0) = 0, f(-1) = -2 and $\frac{f(h) - f(1)}{h} = \frac{4(h-1)}{h}$

4. Let $f: A \rightarrow R$ be given by f(x) = 2 |x| + 3 Where $A = \{-2,0,1,2,\}$, find the range of f. (Ans: $\{3,5,7\}$)

[Q.N.1(b), 2058]

- Check whether the function f = [-2, 3] → R given by f(x) = x³ is one to one, onto or both.
 (Ans: One to one but not onto)
- 6. Let f: R \rightarrow R be defined by y = f(x) = 2x 3, $x \in R$, find formula that defines f^{-1} [Q.N.1(c), 2059]

(Ans: $f^{-1}(x) = \frac{x+3}{2}$)

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7. Let $f: R \rightarrow R$ and $g: R \rightarrow R$ be defined by $f(x) = x^2 + 1$ and $g(x) = x^5$, find f^{-1} , (gof)(x), (fog)(x). [Q.N.7(b), 2059]

Ans: $\begin{cases} f^{-1}(x) = (x-1)^{\frac{1}{2}} \\ (gof)(x) = (x^{2}+1)^{5} \\ \text{and } (fog)(x) = x^{10} + 1 \end{cases}$

8. Define even add odd functions with examples.

[Q.N.1(c), 2060]

9. Let $f: R \to R$ is defined by f(x) = 2x + 3 and $g: R \to R$ is defined by $g(x) = x^2$, find $(g_0f)x$ and $(f_0g)x$.

[Q.N.7(b), 2060]

(Ans: (gof) (x) = $(2x + 3)^2$ and (fog) (x) = $(2x^2 + 3)$

10. Let h: R \rightarrow R be defined by h(x) = 3x - 6, find a formula that defines h⁻¹. [Q.N.1(b), 2061]

(Ans: $h^{-1}(x) = \frac{x-6}{3}$)

- 11. For the functions $f(x) = 2x^2 3$ and g(x) = 3x + 2 where $x \in IR$, determine $f \circ g(x)$, $g \circ f(x)$. Are $(f \circ g)$ and $(g \circ f)$ one—one?

 [Q.N.7(b), 2061]

 (Ans: Not one-one)
- 12. Check whether the function $f: [-2,3] \to \mathbb{R}$ given by $f(x) = x^3$ is one to one, onto or both. [Q.N.1(b), 2062]
- 13. When does an inverse of a function exists ? If $f: \mathbb{R} \to \mathbb{R}$ be defined by $f(x) = x^3 + 5$, find the formula that defines f^{-1} . [Q.N.7(b), 2062]

(Ans: $f^{-1}(x) = \sqrt{x-5}$)

14. Let f, g be real valued function defined as

```
f(x) = x^2 + 5x + 7, x \in R and
        g(x) = 5x - 3, x \in \mathbb{R}
        find fog(x) and gof(x).

(Ans: (25x^2 - 5x + 1) & (5x^2 + 25x + 32))
                                                                                [Q.N.1(b), 2063]
15. Let R be the set of rational numbers. Show that the function defined by
         f: \mathbb{R} \to \mathbb{R} such that f(x) = 4x - 7
        x \in R is one-one and onto. Find a formula for f^{-1}
16.
        Let f, g be real valued functions defined as :
        f(x) = 4x + 7, x \in R and
g(x) = 5x - 2, x \in R
        find fog (x) and gof (x)
                                                                                [Q.N. 1(b), 2064]
        (Ans: (20x - 1) (20x + 33))
17.
         Let Q be the set of all rational numbers. Show that the function:
        f: Q \rightarrow Q such that f(x) = 3x + 5 for all x \in Q is one to one and onto. Find f^{-1}.
                                                                                [Q.N. 7(b), 2064]
        Let f: R \to R be defined by f(x) = 2x + 5. Compute f^{-1}(x).
                                                                               [Q.N. 1(b), 2065]
          Ans: f^{-1}(x) = \frac{x-5}{2}
        If f, g: R\rightarrowR defined by, f(x) = x^3 + 2 and g(x) = 4x - 1, find f(x) and g(x),
19.
        and show that the composite function is not commutative.
                                                                                [Q.N. 7(b), 2065]
900
         Prove that Log_a x^2 - 2 Log_a \sqrt{x} = Log_a x
20.
                                                                               [Q.N.1 (b), 2066]
         Let R be the set of real numbers. Show that the function F: R → R such that
21.
      Af(x) = 5x - 3 for all x \in R is one to one and onto.
                                                                               [Q.N.7 (b), 2066]
         If \frac{\log x}{y-z} = \frac{\log y}{z-x} = \frac{\log z}{x-y}, prove that xyz = 1.
22.
                                                                             2 [Q.N. 1 (b), 2067]
         For the function f(x) = 2x^2 - 3 and g(x) = 3x + 2, x \in R examine whether fog and
23.
         gof are one-one.
         (Ans: both are not one-one)
                                                                            4 [Q.N.7 (b), 2067]
         Define the domain and the range of a function. Find the domain and the range
24.
        of the function f(x) = -x^2 + 4x - 3.
                                                                             [Q.N.11,2068]
         (Ans: Domain = R = (-∞, ∞), Range = (-∞, 1])
        Find the domain of the function y = \sqrt{x-2}.
25.
                                                                        [Q.N. 1(b), Set 'A' 2069]
         [Ans: 2, ∞]
         Draw the graph of the function y = x^2 - 4x + 3 using its different characteristics.
26.
                                                                        [Q.N. 6(b), Set 'A' 2069]
27.
         Define one to one function and onto function. Let a function f: A \rightarrow B be
                               with A = \{-2, -1, 0, 1, 2\} and B = \{0, \frac{1}{6}, \frac{2}{3}\}
         Find the range of f. Is the function f one to one and onto both?
           Ans:0, \frac{1}{6}, \frac{2}{6} and onto only
                                                                         [Q.N. 11, Set 'A' 2069]
        Find the domain, range and inverse of the relation R = {(1, 2), (2, 4), (3, 6), (4, 8)}
                                                                      [Q.N. 1(b), Set 'B' 2069]
         (Ans: {1, 2, 3, 4}, { 2, 4, 6, 8}, {(2, 1), (4, 2), (6, 3), (8, 4)}
         Define function. State the condition for a function to be bijective. Given
         f(x) = x^3 + 5, x \in R, find f^{-1}
                                                                         [Q.N. 11, Set 'B' 2069]
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(Ans: $f^{-1}(x) = \sqrt[3]{x-5}$)

- 30. Solve the inequality $|2x + 1| \ge 3$ and draw its graph. [Q.N. 6(a) (Or), Supp. 2069]
- 31. Define composite function of $f = R \rightarrow R$ and $g = R \rightarrow R$ be defined by $f(x) = 3x^2 4$ and g(x) = 2x 5. find (gof) (x), (fog) (x) and (fof) (x). Is (gof) x = (fog) x? Is the composite function (gof) (x) one to one? Give reason. [Q.N. 11, Supp. 2069] (Ans: $6x^2 13$, $12x^2 60x + 71$, $3x^4 24x^2 + 44$, not one to one)
- 32. Let a function f: $A \to B$ be defined by $f(x) = \frac{x+1}{2x-1}$. Find the range of f. Is the function f one to one and onto both? If not, how can the function be made one to one and onto both?

 [Q.N. 11, 2070 'C']

 (Ans: $R \left\{\frac{1}{2}\right\}$; one to one only)
- 33. Solve the inequality: $6 + 5x x^2 \ge 0$. [Q.N. 6(a)(Or), 2070 'D'] (Ans: $\{x : -2 \le x \le 3\}$)
- Define composite function of two functions f and g. Let $f:R \to R$ and $g:R \to R$ be two functions defined by $f(x) = 2x^2 3$ and g(x) = 3x + 2. Determine (fog) (x), (gof) (x) and (gog) (x). Is (fog) (x) = (gof) (x)? Are the functions (fog) (x) and (gog) (x) one to one?

 [Q.N. 11, 2070 'D']

 (Ans. $18x^2 + 24x + 5$, $6x^2 7$, 9x + 8, not one to one)

Unit 3 - Curve Sketching

- 1. Test the periodicity and the symmetricity of the function $y = \sin x$. [Q.N.(c),2068]
- 2. Draw the graph of $y = \cos x \left(-\frac{\pi}{2} \le x \le \frac{\pi}{2} \right)$ using its different characteristics.

3.

- Test the periodicity of the function $f(x) = \sin 2x$ and find its period.
- [Q.N. 1(c), Set 'A' 2069] If $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$, show that: $x^2 + y^2 + z^2 + 2xyz = 1$ [Q.N. 7(a), Set 'A' 2069]
- 5. State sine law. Prove that: $\tan \frac{1}{2} (B-C) = \frac{b-c}{b+c} \cot \frac{A}{2}$.

 [Q.N. 7(a)(Or), Set 'A' 2069]
- Examine the function y = cosx for symmetry and even or odd nature.

 [Q.N. 1(c), Set 'B' 2069]
- 7. Sketch the graph of $f(x) = (x 4)^2 8$ indicating its characteristics.
- [Q.N. 6(b), Set 'B' 2069] 8 Test the periodicity of the function $f(x) = \cos \pi x$ and find its period.
- (Ans: 2) [Q.N. 1(c), Supp. 2069]
- Draw the graph of the function $f(x) = x^2 2x 3$ with its different characteristics. [Q.N. 6(b), Supp. 2069]
- [Q.N. 6(b), Supp. 2069
- $f(x) = \frac{e^X e^{-X}}{e^X + e^{-X}}$ is even or odd. Also examine for its symmetricity.
- (Ans: f(x) is odd function, symmetric about origin)
 11. Using different characteristics, sketch the graph of $y = -x^2 + 4x 3$.

 [Q.N. 6(b), 2070 'C']
- 12. Test the even or odd nature and the symmetricity of the function f(x) = x⁴ + 3x² + 1. [Q.N. 1(c), 2070 'D']
- (Ans: even, symmetric about y-axis)

 Using different characteristics, sketch the graph of y = (x 1) (x 2) (x 3).

 [Q.N. 6(b), 2070 'D']
- Determine whether the function $f(x) = \sqrt{x^2 1}$ is even or odd. Also test its symmetricity.

 [Q.N. 1(c), 2071 'C']

 (Ans: even function, symmetric about y-axis))

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- Sketch the graph of $y = -x^2 + 4x 3$ indicating its characteristics. [Q.N.6(b),2071 'C'] 15.
- 16.
- Define even and odd functions and give example of each. [Q.N. 1(c), 2071 'D'] Sketch the graph of $y = x^2 + 5x + 4$ indicating its characteristics. [Q.N.6(b),2071 'D']

Unit 4 - Trigonometry

4.1 **Inverse Circular Function**

Find the value of $tan^{-1}3 + tan^{-1}\frac{1}{3}$ [Q.N.2(a), 2056]

 $\left(\operatorname{Ans}:\frac{\pi}{2}\right)$

Solve: $\sin^{-1} \frac{2a}{1+a^2} + \sin^{-1} \frac{2b}{1+b^2} = 2 \tan^{-1} x$. [Q.N.8(a), 2056]

Ans: x = a + b

- Prove that : Sin (2 Sin⁻¹x) = 2x $\sqrt{1-x^2}$
- Find the value of Cos tan-1 Sin Cot-1 x. [Q.N.8(a) (Or), 2057] Distil 2 - Curve Shell

Find the value of tan 3 + tan 5. [Q.N.2(a), 2058]

 $\left(\text{Ans: } \frac{\pi}{2} \right)$

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- Prove that $\cot^{-1} 3 + \csc^{-1} \sqrt{5} = \frac{\pi}{4}$ [Q.N.8(a), 2058]
- Show that $\tan^{-1}\frac{1}{5} + \tan^{-1}\frac{1}{7} = \tan^{-1}\frac{6}{17}$. 7. [Q.N.2(a), 2059]
- Prove: $tan (2 tan^{-1} x) = 2 tan (tan^{-1} x + tan^{-1} x^3)$ 8. [Q.N.8(a), 2059]
- Show that $\tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{3} = \frac{\pi}{4}$. [Q.N.2(a), 2060]
- Prove that $\cot^{-1} (\tan 2x) + \cot^{-1} (\tan 3x) = x$. [Q.N.8(a), 2060]
- Solve: $2\tan^{-1} x = \sin^{-1} \frac{2m}{1 + m^2} + \sin^{-1} \frac{2n}{1 + n^2}$ 11. [Q.N.2(a), 2061]

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(Ans. even uncilon, syst-neino abust

- If $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \pi$, prove that x + y + z = xyz. [Q.N.8(a), 2061]
- Solve: $Cos(Sin^{-1}x) = \frac{1}{2}$ 13. [Q.N.2(a), 2062]

Ans: $x = \frac{\sqrt{3}}{2}$

- (Ans. 1(x) is odd fenction, symmetric ybout orig Solve: Tan²x = Secx+1; designed in the second section of the [Q.N.8(a) (Or), 2062] 14. Ans: $(6n\pi \pm 1)\frac{\pi}{3}$ or $(2n + 1)\pi$
- Prove that: $tan^{-1} \left(\frac{\sin x}{1 + \cos x} \right) = \frac{x}{2}$ risixe y reode sime arrye me [Q.N.2(a), 2063] 15.
- 16. Prove that: $\tan^{-1}1 + \tan^{-1}2 + \tan^{-1}3 = 2(\tan^{-1}1 + \tan^{-1}\frac{1}{2} + \tan^{-1}\frac{1}{3}).$

[Q.N.8(a) (Or), 2060]

17. Prove that:
$$\tan^{-1}\left(\frac{a-b}{1+ab}\right) + \tan^{-1}\left(\frac{b-c}{1+bc}\right) + \tan^{-1}\left(\frac{c-a}{1+ca}\right) = 0$$
[Q.N. 2(a), 2064]
18. Prove that: $\sec^{-1}x + \csc^{-1}x = \frac{\pi}{2}$
[Q.N. 2(a), 2065]
19. If $\tan^{-1}x + \tan^{-1}y + \tan^{-1}z = \pi$, show that $x + y + z = xyz$.
[Q.N. 8(a), 2065]
20. Prove that $\cos^{-1}(-x) = \pi - \cos^{-1}x$
[Q.N. 2(b), 2066]
21. If $\cot^{-1}x + \cot^{-1}y + \cot^{-1}z = \pi$ show that $xy + yx + zx = 1$
[Q.N. 2 (a), 2067]
22. Show that $\tan^{-1}x = \frac{1}{2}\sin^{-1}\frac{2x}{1+x^2}$
23. If $\sin^{-1}x + \sin^{-1}y + \sin^{-1}z = \pi$, prove that $x + y + x + z = 1$
24. Prove that: $\tan^{-1}x + \tan^{-1}x + \tan^{-1}x$

Solve for general values of x: $7 \sin^2 x + 3 \cos^2 x = 4$.

Ans: $x = n\pi \pm \frac{\pi}{6}$

5.

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6. Solve for general values of x: $\cos x + \cos 2x + \cos 3x = 0$ [Q.N.8(a) (Or), 2061] $x = (2n + 1)\frac{\pi}{4}$ and x = (6n ± 2) $\frac{\pi}{3}$ 7. Solve: $\cos 3x + \cos 2x = \sin \frac{3}{2}x + \sin \frac{x}{2}$, $0 \le x \le \pi$. [Q.N.8(a), 2062] (Ans: Values of x in the internal $[0, \pi]$ are $\frac{\pi}{7}, \frac{5\pi}{7}, \pi$) Find the general values of x, when Sin2xtanx + 1 = Sin2x + tanx[Q.N.8(a), 2063] Ans: (4n + 1) Find the general values of x when Cos x + Sin x = Cos 2x + Sin 2x9. [Q.N. 8(a), 2064] Ans: $2n\pi$, $(4n + 1)\frac{\pi}{6}$ fibi + i Tobi If $\sin 2x = 3 \sin 2y$, prove that : 2 tan $(x-y) = \tan (x + y)$ [Q.N. 8(a)(or), 2064] Solve: $Sin\theta + Sin2\theta + Sin3\theta = Cos\theta + Cos2\theta + Cos3\theta$ 11. [Q.N. 8(a, or), 2065] Ans: $(6n \pm 2)\frac{\pi}{3}$, $(4n + 1)\frac{\pi}{8}$ Solve for general values of θ : tan $(\theta + \alpha)$, tan $(\theta - \alpha) = 1$. 12. Ans: $(2n + 1)\frac{\pi}{4}$ [Q.N.8 (a) (or), 2066] 13. Solve for general values of x: $2 \sin^2 x + \sin^2 2x = 2$ 4 [Q.N.8 (a) (Or), 2067] Ans: $x = \left(2n\pi \pm \frac{\pi}{2}\right)$ Solve: $\cot x + \tan x = 2 \ (0 \le x \le \pi)$ 14. [Q.N.2(a),2068] Ans: $\frac{\pi}{4}$ 15. Solve: $\sin x - \cos x = \sqrt{2}$. Ans: $x\pi + (-1)^n \frac{\pi}{2} +$ [Q.N. 2(a), Set 'A' 2069] 16. Solve: $\tan 2x = \tan x (-\pi \le x \le \pi)$. [Q.N. 2(a), Set 'B' 2069] (Ans: $0, \pm \pi$) 17. Solve: $2\cos^2 x + 4\sin^2 x = 3$. [Q.N. 2(a), Supp. 2069] Ans: nπ ± 18. Solve : $\sin x + \cos x = \sqrt{2}$ $(-2\pi \le x \le 2\pi)$. [Q.N. 7(a), 2070 'C'] $\left(\text{Ans:} -\frac{7}{4}, \frac{7}{4}\right)$ Solve: $\sin^2\theta - 2\cos\theta + \frac{1}{4} = 0$. 19. [Q.N. 7(a), 2070 'D'] (Ans: $(6n \pm 1) \frac{\pi}{2}$ 20. Solve for x: tan2x = tanx. [Q.N. 2(a), 2071 'C'] (Ans: $x = n\pi$) 21. Solve: $\sqrt{3} \sin x - \cos x = \sqrt{3} \text{ for } 0 \le x \le 2\pi$. av intenen tol sylot [Q.N. 2(a), 2071 'D']

Properties of a Triangle

- [Q.N.1(c), 2056] Prove that $r_1r_2 + rr_3 = ab$
- If $a^4+b^4+c^4=2c^2(a^2+b^2)$ prove that $\angle C=45^\circ$ or 135° [Q.N.8(b), 2056]
- [Q.N.1(c), 2057] 3.
- If S be the area of incircle and S1, S2, S3 are areas of excircles

Show that:
$$\frac{1}{\sqrt{S_1}} + \frac{1}{\sqrt{S_2}} = \frac{1}{\sqrt{S}} - \frac{1}{\sqrt{S_3}}$$
 [Q.N.8(b), 2057]

- Prove that $\frac{1}{2} + \frac{1}{2}$ [Q.N.1(c), 2058]
- In any ABC prove that, [Q.N.8(b), 2058] SinB SinC
- [Q.N.1(b), 2059]
- In any triangle ABC prove: $\tan \frac{1}{2}(B-C) = \frac{B-C}{b+C} \cot \frac{A}{2}$.
- In any triangle ABC, prove that SinA + SinB + Sin C = $\frac{S}{D}$ [Q.N.1(b), 2060]
- 10. Prove that, in any triangle ABC,

$$\frac{b^2 - c^2}{a^2}$$
. Sin2A + $\frac{c^2 - a^2}{b^2}$. Sin 2B + $\frac{a^2 - b^2}{c^2}$. Sin 2C = 0 [Q,N.8(b), 2060]

- In any triangle ABC, if CosB = $\frac{SinA}{2SinC}$, show that the triangle is isosceles. 11.
 - [Q.N.1(c), 2061] In any triangle ABC, prove that
- 12. $b^2 Sin (C - A) c^2 Sin (A - B)$ a2 Sin (B - C)
- [Q.N.8(b), 2061] SinB + Sin C + Sin C + Sin A + Sin B [Q.N.1(c), 2062]
- Prove that $r r_1 r_2 r_3 = \Delta^2$ 13. In any $\triangle ABC$, prove that : $\frac{\cos B - \cos C}{\cos A + 1}$ [Q.N.8(b), 2062] 14.309
- In a ABC, prove that : 15.
- [Q.N.1(c), 2063] (b+c) CosA + (c+a) CosB + (a+b) CosC = a+b+c
- [Q.N.8(b), 2063] In any triangle, prove that $r_1 + r_2 + r_3 - r = 4R$
- In a \triangle ABC, prove that $\frac{c + b \cos A}{b c \cos A} = \frac{\cos B}{\cos C}$ [Q.N. 1(c), 2064] 17.
- 18. In any triangle, prove that: [Q.N. 8(b), 2064] a cos A + b cos B + c cos C = 4 R sin A sin B sin C
- Show that $\frac{1}{r_1}$ [Q.N. 1(c), 2065] 19.
- [Q.N. 8(b), 2065] 20. In any triangle, state and prove Cosine law
- 21. [Q.N.1 (c), 2066]
- 22. In a △ABC, if (sinA + sinB + sinC) (sinA + sinB - sinC) = 3sinA SinB then prove ∠C=60°. [Q.N.8 (b) (Or), 2066]
- sinA In any triangle if $\cos B = \frac{\sin A}{2\sin C}$, prove that the triangle is isosceles. 23.
- 2 [Q.N. 1 (c), 2067] In any triangle ABC if $8R^2 = a^2 + b^2 + c^2$, prove that the triangle is right angled. 24.
 - 4 [Q.N.8 (b) (Or), 2067]

25. State Cosine Law, using Cosine Law stansing a resignment

Prove that:
$$\cos \frac{A}{2} = \sqrt{\frac{s(s-a)}{bc}}$$
 [Q.N.7(a)(Or),2068]

26. If $\frac{1}{a+c} + \frac{1}{b+c} = \frac{2}{a+b+c}$, show that $c = 60^{\circ}$. [Q.N. 7(a) (Or), Supp. 2069]

27. State sine law. Using sine law, prove that: $\tan \frac{1}{2} (C - A) = \frac{c - a}{c + a} \cdot \cot \frac{B}{2}$ [Q.N. 7(a)(Or), 2070 'C']

28. If $a^4 + b^4 + c^4 = 2c^2(a^2 + b^2)$, prove that: $C = 45^\circ$ or 135°. [Q.N. 7(a)(Or), 2070 'D'] 29. State sine law. Use this law to prove the projection law. [Q.N. 7(a)(Or), 2071 'C']

30. In any triangle ABC, if $\frac{\cos A + 2\cos C}{\cos A + 2\cos B} = \frac{\sin B}{\sin C}$, then prove that the triangle is either isosceles or right angled. [Q.N. 7(a)(Or), 2071 'D']

4.4 Solution of a Triangle

1. If three sides of a triangle are in the ratio 2: $\sqrt{6}$: $\sqrt{3}$ +1, find the angles. [Q.N.8(b) (Or), 2056]

(Ans: A = 45°, B = 60° and C = 75°)

2. Solve the triangle if $a = \sqrt{6}$, b = 2 and $c = \sqrt{3} - 1$. [Q.N.8(b) (Or), 2057] (Ans: $A = 120^{\circ}$, $B = 45^{\circ}$, $C = 15^{\circ}$)

3. If a = 2, $b = \sqrt{6}$, $c = \sqrt{3} + 1$, solve the triangle. (Ans: $A = 45^\circ$, $B = 60^\circ$, $C = 75^\circ$)

4. Solve the triangle, if a = 2, $b = \sqrt{6}$, $c = \sqrt{3} + 1$. (a. [Q.N.8(b) (Or), 2059] (Ans: $A = 45^{\circ}$, $B = 60^{\circ}$ and $C = 75^{\circ}$)

In any triangle ABC,
 b = √3, C = 1 and A = 30°
 solve the triangle.

[Q.N.8(b) (Or), 2060]

any triangle ABC. If CosB

(Ans: a = c = 1, $b = \sqrt{3}$, $\angle A = \angle C = 30^{\circ}$, $\angle B = 120^{\circ}$)

6. In any triangle ABC, if A = 30° and B = 90°, find a : b : c [Q.N.8(b) (Or), 2061]

(Ans: $\frac{1}{2}$: 1: $\frac{\sqrt{3}}{2}$)

7. In any $\triangle ABC$, a = 2, $b = \sqrt{6}$ and $c = \sqrt{3} - 1$, find $\angle B$ [Q.N.8(b)-(Or), 2062] (Ans: $\angle B = 60^{\circ}$)

If the angles of a triangle are to one another as 1:2:3, prove that the corresponding sides are $1:\sqrt{3}:2$. [Q.N. 8(b)(or), 2064]

9. In any triangle ABC, $b = \sqrt{3}$, c = 1 and $\angle A = 30^\circ$, solve the triangle. [Q.N. 8(b), (Or), 2065]

10 If A=30°, B=45°, a=6 $\sqrt{2}$, solve the triangle ABC. (Ans: b = 12, c = 6($\sqrt{3}$ + 1), C = 105°) [Q.N.8 (b), 2066]

11. In any triangle ABC, $b = \sqrt{3}$, C = 1 and $A = 30^{\circ}$, solve the triangle. (Ans: a = c = 1, $b = \sqrt{3}$, $\angle A = \angle C = 30^{\circ}$, $\angle B = 120^{\circ}$)

12. If a = 2, $b = 1 + \sqrt{3}$, $C = 60^\circ$, solve the triangle ABC. [Q.N. 7(a)(Qr), Set 'B' 2069] (Ans: a = 2, $b = 1 + \sqrt{3}$, $c = \sqrt{6}$, $A = 45^\circ$, $B = 75^\circ$, $C = 60^\circ$)

Unit 5 – Sequence and Series, and Mathematical Induction

1. Using the principle of mathematical induction, prove that: $1 + 2 + 3 + 4 + \dots + n = \frac{n(n+1)}{2}$

[Q.N.2(b),2068]

n(n + 1) (2n + 1)Prove that: $1^2 + 2^2 + 3^2 + 4^2 + \dots + n^2 =$ [Q.N.12,2068] Use the principle of mathematical induction: 3. $2 + 4 + 6 + \dots + 2n = n(n+1).$ [Q.N. 2(b), Set 'A' 2069] Find the sum of n terms of the series $3.1^2 + 4.2^2 + 5.3^2$ Ans: $\frac{1}{12}$ n(n + 1) (3n² + 11n + 4) [Q.N. 12, Set 'A' 2069] Prove by the principle of mathematical induction. 5. $2 + 4 + 6 \dots + 2n = n(n+1)$. [Q.N. 2(b), Set 'B' 2069] 6. Find the nth term and then the sum of the first n-terms of the series: $1^2.2 + 2^2.3$ + 32.4 + [Q.N. 12, Set 'B' 2069] Ans: n3 + n2: n(n + 1) (3n2 + 5n + 1) Using principle of mathematical induction, prove that: 7. $2+2^{2}+2^{3}+\dots+2^{n}=2(2^{n}-1)$ The sum of an infinite number of terms in G.S. is 15, and the sum of their squars [Q.N. 12, Supp. 2069] is 45: find the series. Ans: $5 + \frac{10}{3} + \frac{20}{9} + \dots$ Using principle of mathematical induction, prove that: $1 + 3 + 5 + 7 + \dots + (2n - 1) = n^2$. [Q.N. 2(b), 2070 'C'] Show that the A.M., G.M. and H.M. between any two unequal positive numbers 10. satisfy the following relations. a) $(G.M.)^2 = A.M. \times H.M.$ [Q.N. 12, 2070 'C'] b) A.M. > G.M. > H.M. Using principle of mathematical induction, 11. prove that: $\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{8}$ [Q.N. 2(b), 2070 'D'] Sum to infinity the following series. $1 - 5a + 9a^2 - 13a^3 + \dots$ to ∞ (-1 < a < 1). [Q.N. 12, 2070 'D'] Prove by mathematical induction: . 13. [Q.N. 2(b), 2071 'C'] $1 + 3 + 5 + \dots + n \text{ terms} = n^2$ Sum to n terms of the series: $\frac{2}{5} - \frac{6}{52} + \frac{10}{53} - \frac{14}{54} + ...$ [Q.N. 12, 2071 'C'] 14. Prove by the principle of mathematical induction that: 15. 4ⁿ-1 is divisible by 3. [Q.N. 2(b), 2071 'D'] Sum to n terms of the series: 1. n + 2. (n - 1) + 3. (n - 2) + ...ns: n(n + 1) (n + 2) [Q.N. 12, 2071 'D'] Unit 6 - Matrices and Deter

1. Let $A = \begin{pmatrix} 1 & 3 \\ 2 & 4 \end{pmatrix}$ and $B = \begin{pmatrix} 5 & 7 \\ 6 & 8 \end{pmatrix}$ then prove $AB \neq BA$. [Q.N.3(a), 2056]

Evaluate 1 + X 1 1 1 1 + y 1 [Q.N.10(a), 2056]

(Ans: xyz + yz + zx + xy)

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3. Let
$$A = \begin{pmatrix} 1 & 3 \\ 2 & 4 \end{pmatrix}$$
 and $B = \begin{pmatrix} 3 & 2 \\ 1 & 4 \end{pmatrix}$ find the transpose of AB. [Q.N.3(a), 2057]
(Ans: $\begin{pmatrix} 6 & 10 \\ 14 & 20 \end{pmatrix}$)

4. Find the value of:
$$\begin{vmatrix} 1 & bc & a(b+c) \\ 1 & ca & b(c+a) \\ 1 & ab & c(a+b) \end{vmatrix}$$
 [Q.N.10(a), 2057]

(Ans: 0) 5. Let $A = \begin{pmatrix} 2 & 1 \\ 0 & 7 \end{pmatrix}$ and $B = \begin{pmatrix} 1 & 5 \\ 3 & 2 \end{pmatrix}$,

Find (AB) T [Q.N.3(a), 2058]

6. If $A = \begin{pmatrix} 1 & 2 \\ 3 & 1 \end{pmatrix}$, show that $A^2 - 2A - 5I = 0$, [Q.N.10(a), 2058]

7. Let $A = \begin{pmatrix} 1 & 3 \\ 2 & 4 \end{pmatrix}$ and $B = \begin{pmatrix} 5 & 7 \\ 6 & 8 \end{pmatrix}$, find $(AB)^T$. [Q.N.3(a), 2059]

(Ans: (31 46))

8. Evaluate a b c a [Q.N.10(a), 2059]

(Ans: (a-b) (b-c) (c-a) (a+b+c)) 9. $A = \begin{pmatrix} 2 & 0 \\ 1 & 3 \end{pmatrix}$ and $B = \begin{pmatrix} -2 & 1 \\ 3 & 2 \end{pmatrix}$, show that $(AB)^T = B^T A^T$. [Q.N.3(a), 2060]

10. Use properties of determinant to show that

 $\begin{vmatrix} 1 & x & x^2 \\ 1 & y & y^2 \\ 1 & z & z^2 \end{vmatrix} = \begin{vmatrix} 1 & x & yz \\ 1 & y & zx \\ 1 & z & xy \end{vmatrix}$

[Q.N.10(a), 2060]

11. Construct a 3×3 matrix whose elements are $a_{ij} = 2i + j$. [Q.N.3(a), 2061]

 $\left(\mathsf{Ans:} \left(\begin{array}{ccc} 3 & 4 & 5 \\ 5 & 6 & 7 \\ 7 & 8 & 9 \end{array}\right)\right)$

12. Without expanding show that :

 $\begin{vmatrix} 1 & bc & b+c \\ 1 & ca & c+a \\ 1 & ab & a+b \end{vmatrix} = \begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$

[Q.N.10(a), 2061]

13. If $A = \begin{pmatrix} 2 & 0 \\ 1 & 3 \end{pmatrix}$ and $B = \begin{pmatrix} -2 & 1 \\ 3 & 2 \end{pmatrix}$, show that $(AB)^T = B^TA^T$ [Q.N.3(a), 2062]

14. Prove that : | a-b-c 2a 2a | 2b b-c-a 2b | = (a+b+c)³ [Q.N.10(a), 2062]

15. Define a triangular matrix. How do you distinguish between upper and lower triangular matrixes? [Q.N.3(a), 2063]

Prove (without expanding).

 $\begin{vmatrix} bc & a & a^2 \\ ca & b & b^2 \\ ab & c & c^2 \end{vmatrix} = \begin{vmatrix} 1 & a^2 & a^3 \\ 1 & b^2 & b^3 \\ 1 & c^2 & c^3 \end{vmatrix}$ [Q.N.10(a), 2063]

17. If
$$A = \begin{bmatrix} 3 & 2 \\ 2 & 1 \end{bmatrix}$$
, find A^{-1}

[Q.N. 4(b), 2064]

$$\left(\mathsf{Ans}: \left(\begin{array}{cc} -1 & 2 \\ 2 & -3 \end{array}\right)\right)$$

18. Prove (without expanding):

$$\begin{vmatrix} 1 & bc & b+c \\ 1 & ca & c+a \\ 1 & ab & a+b \end{vmatrix} = \begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$$

[Q.N. 10(a), 2064]

Define symmetric and skew symmetric matrix with examples. [Q.N. 3(a), 2065

20. Show that :
$$\begin{vmatrix} x^2 + 1 & xy & xz \\ xy & y^2 + 1 & yz \\ xz & yz & z^2 + 1 \end{vmatrix} = 1 + x^2 + y^2 + z^2$$
 [Q.N. 10(a), 2065]

21. If
$$A + B = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$$
 and $A - 2B = \begin{bmatrix} -1 & 1 \\ 0 & -1 \end{bmatrix}$ then determine the marix A.

$$\left(\begin{array}{c|c}
 & 1 & 1 \\
 & 3 & 3 \\
 & 2 & 1 \\
 & 3 & 3
\end{array} \right)$$

[Q.N.3 (a), 2066]

22. If a, b, c are non zero and
$$\begin{vmatrix} a & a^3 - 1 \\ b & b^2 & b^3 - 1 \\ c & c^2 & c^3 - 1 \end{vmatrix} = 0$$
, then show that abc = 1.

[Q.N.10 (a), 2066]

23. Construct (3 \times 3) matrix with the elements given by $a_{ij} = 2i + j$.

2 [Q.N. 3 (a), 2067]

24. Prove that :
$$\begin{vmatrix} a & b & ax + by \\ b & c & bx + cy \\ ax + by & bx + cy & 0 \end{vmatrix} = (b^2 - ac)(ax^2 + 2bxy + cy^2)$$

4 [Q.N.10 (a), 2067]

25. Find the inverse of the matrix
$$A = \begin{pmatrix} 7 & -3 \\ 6 & 2 \end{pmatrix}$$
 [Q.N.2(c),2068]

$$\left(\text{Ans:} \frac{1}{32} \left(\begin{array}{cc} 2 & 3 \\ -6 & 7 \end{array}\right)\right)$$

26. Show that:
$$\begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ yz & zx & xy \end{vmatrix} = (x - y) (y - z) (z - x) (xy + yz + zx)$$
 [Q.N.7(b),2068

27. If
$$A = \begin{pmatrix} 4 & -5 \\ 3 & 6 \end{pmatrix}$$
 and $B = \begin{pmatrix} 2 & 3 \\ -1 & -2 \end{pmatrix}$ find $(AB)^T$.

$$\left(\text{Ans:} \begin{array}{cc} 13 & 4 \\ 22 & 3 \end{array}\right)$$

[Q.N. 2(c), Set 'A' 2069]

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28. Show that:
$$\begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ b+c & c+a & a+b \end{vmatrix} = (b-c)(c-a)(a-b)(a+b+c).$$

29. For the given matrices $A = \begin{pmatrix} 1 & 2 \\ 2 & 5 \end{pmatrix}$ and $B = \begin{pmatrix} 5 & -2 \\ -2 & 1 \end{pmatrix}$, [Q.N. 7(b), Set 'A' 2069]

so that: (A + B) = A' + B'.

[Q.N. 2(c), Set 'B' 2069]

30. Without expanding show that: $\begin{vmatrix} 1 & bc & a(b+c) \\ 1 & ca & b(c+a) \\ 1 & ab & c(a+b) \end{vmatrix} = 0.$

[Q.N. 7(b), Set 'B' 2069]

31. If A = $\begin{pmatrix} 5 & 3 \\ 4 & 2 \end{pmatrix}$, find Adj. A. [Q.N. 2(c), Supp. 2069]

 $\left(\operatorname{Ans}: \left(\begin{array}{cc} 2 & -3 \\ -4 & 2 \end{array}\right)\right)$

32. Prove that : $\begin{vmatrix} a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = (b-c) (c-a) (a-b) (a+b+c)$. [Q.N. 7(b), Supp. 2069]

33. If $A = \begin{pmatrix} 2 & 1 \\ 1 & -2 \\ 1 & -2 \end{pmatrix}$, find AA^T d G d beauties from [Q.N. 2(c), 2070 'C']

 $\begin{array}{c} \text{360S} & \left(\begin{array}{c} 4 \text{ns.} \left(\begin{array}{c} 5 & 0 \\ 0 & 5 \end{array} \right) \right) \\ \text{3 a}^2 \text{ b vid b cig. c}^2 + \text{ac. salt risks whiten } (8 \times 8) \text{ so where } 3 \end{array} \right) \end{array}$

34. Prove that: $a^2 + ab b^2 ac = 4a^2b^2c^2$ [Q.N. 7(b), 2070 'C']

35. If $A = \begin{pmatrix} 4 & -5 \\ 3 & 6 \end{pmatrix}$ and $B = \begin{pmatrix} 2 & 3 \\ -1 & -2 \end{pmatrix}$, fid B^TA^T . [Q.N. 2(c), 2070 'D']

36. Prove that: $\begin{vmatrix} a+x & b & c \\ a & b+y & c \\ a & b & c+z \end{vmatrix} = xyz \left(1 + \frac{a}{x} + \frac{b}{y} + \frac{c}{z}\right)$ [Q.N. 7(b), 2070 'D']

37. Define singular matrix. Test whether the matrix if $A = \begin{pmatrix} 3 & 1 & 0 \\ -2 & 1 & -1 \\ -1 & 3 & -2 \end{pmatrix}$ is singular or not. [Q.N. 2(c), 2071 'C']

(Ans: Singular) TV + VX) (x - x) (x - x) (x - x) = XV Without expanding the determinant show that;

 $\begin{vmatrix} 1 & a^2 & a^3 \\ 1 & b^2 & b^3 \\ 1 & c^2 & c^3 \end{vmatrix} = \begin{vmatrix} a^2 & bc & a \\ b^2 & ca & b \\ c^2 & ab & c \end{vmatrix}$ [Q.N. 7(b), 2071 'C']

39. If $A = \begin{pmatrix} 2 & 3 \\ 5 & -2 \end{pmatrix}$, show that: $A^{-1} = \frac{1}{19} A$. [Q.N. 2(c), 2071 'D']

V+Z V Z Z+X Z X Without expanding the determinant show that: [Q.N. 7(b), 2071 'D'] Unit 7 - System of Linear Equations [Q.N.3(b), 2056] Solve by Cramer's rule: -x + y = 9, x - 3y = 5(Ans: x = -16 and y = -7) Solve by row equivalent matrix method: x + z = 1; z + 2y = 2; 5x - 9y = -32. [Q.N.10(b), 2056] (Ans: x = 3, y = 2 and z = -2) Solve by using inverse matrix method: x - y = 2; 2x + 3y = 9 (S- = x bne s = [Q.N.10(b) (Or), 2056] (Ans: x = 3, y = 1)Solve by Cramer's rule: 2x - y = 5; x - 2y = 1. 4. (Ans: x = 3, y = 1)Solve by using row equivalent matrix method: [Q.N.10(b), 2057] x - 2y + 2z = 0; x - 2y + 3z = -1; 2x - 2y + z = -3(Ans: x = -4, y = -3, z = -1) Solve by inverse matrix method: -2x + 4y = 3 and x all [Q.N.10(b) (Or), 2057] 3x - 7y = 1Solve by Cramer's rule of the business was selected as the sel 7. x - 2y = -7[Q.N.3(b), 2058] 3x + 7y = 5(Ans: x = -3, y = 2) Solve, by row equivalent matrix method, X+V+Z=1x + 2y + 2z = 4[Q.N.10(b), 2058] x + 3y + 7z = 13(Ans: x = 1, y = -3, z = 3) Solve by inverse matrix method, 2x + 5y = 7, 5x + 2y = 3 vol vo - o tsuo [Q.N.10(b) (Or), 2058] (Ans: $x = \frac{-29}{21}$, $y = \frac{41}{21}$) Solve by Cramer's rule 2x - y = 5; [Q.N.3(b), 2059] 10. x - 2y = 1. (Ans: x = 3, y = 1)Solve by row equivalent matrix method x + z = 1; 5x - 9y = -3. oniem xitiam [Q.N.10(b), 2059] (Ans: x = 3, y = 2, z = -2) Solve by using inverse matrix method: $2x + 4y = 7 \\ 8x - 6y = -5$ [Q.N.10(b) (Or), 2059] 12. Ans: $x = \frac{1}{2}$ and $y = \frac{3}{2}$ 13. Give reason why simultaneous equation x + 2y = 5 and 3x + 6y = 12 are not [Q.N.3(b), 2060] solvable by Cramer's rule. Solve, by row equivalent matrix method: 14. x - 2y - 3z = -1, 2x + y + z = 6, x + 3y - 2z = 13. [Q.N.10(b), 2060] (Ans: x = 2, y = 3 and z = -1) Solve by matrix inversion method 3x + 5y = 7, 5x + 9y = 7. [Q.N.10(b) (Or), 2060] 15.

(Ans: x = 14 and y = -7)

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   16.
                  Solve by matrix inversion method, x + y = 2 and x - y = 0.
                                                                                                                                      [Q.N.3(b), 20611
                 (Ans: x = 1 and y = 1)
                 Solve by Cramer's rule: 18 1. world that imperso and palabasaxe augment
   17.
                 x + 2y + 3z = 6, 2x + 4y + z = 7 and 3x + 2y + 9z = 14.
                                                                                                                                    [Q.N.10(b), 2061]
                 (Ans: x = 1, y = 1 and z = 1)
                 Solve by Row-equivalent matrix method :
                 x-y-z=-2, x+4z=4 and y-2z=1.
                                                                                                                         [Q.N.10(b) (Or), 2061]
                                                                    MILL TO CHOLONY OF THE
  19.
                Solve: x = 2y + 3 and 3x - 5y = 8 by inverse matrix method. [Q.N.3(b), 2062]
                (Ans: x = 1 and y = -1)
                                                                                                  (Year Voite 31 -- a
  20.
                Solve by row- equivalent method:
                9y - 5x = 3.
                x + z = 1 and
                z + 2y = 2
                                                                                                                                   [Q.N.10(b), 2062]
                (Ans: x = 3, y = 2 and z = -2)
 21. Solve the equations by Cramer's rule : Solve the equations of the equation of the equations of the equation of the equations of the equation of the
                9y - 5x = 3
                x + z = 1 and z + 2y = 2
  z + 2y = 2
                                                                                                                           [Q.N.10(b) (Or), 2062]
                (Ans: x = 3, y = 2 and z = -2)
 22.
                Solve by Inverse matrix method:
                       3x + 2y = 5
                       7x + 5y = 12
                                                                                                                               [Q.N.4(b), 2063]
                (Ans: x = 1, y = 1)
               Solve by Cramer's rule or by row equivalent matrix method: 3 9 9 9 9
 23.
                         X+V+Z=6
 x-y+z=2
                        2x + y - z = 1
                                                                                                                                 [Q.N.10(b), 2063]
               (Ans: x = 1, y = 2, z = 3)
 24.
               Solve by row-equivalent method:
               3x - 2y = 8
               5x + 3y = 7
                                                                                                                               [Q.N. 3(a), 2064]
               (Ans: 2, -1)
25. Solve the following system of equations by inverse matrix method or Cramer's
               2x - y + 3z = 9, x + y + z = 6, x - y + z = 2.
                                                                                                                                 [Q.N. 10(b), 2064]
               (Ans: 1, 2, 3)
26. Solve by Cramer's rule :
                                    3x + 2y = 8
                                    4x + y = 9
                                                                                                                                   [Q.N. 3(b), 2065]
               (Ans: x = 2, y = 1)
27. Solve by matrix method :
                                    x+y+z=6
                                    Salva by using inverse cratic method as - 82 - 82 - 82
                                    2x + y - z = 1
                                                                                                                                 [Q.N. 10(b), 2065]
              (Ans: x = 1, y = 2, z = 3)
28.
              Solve by cramer's rule: -x + y = 9, x - 3y = 5
              (Ans: (-16, -7))
                                                                                                                                  [Q.N.3 (b), 2066]
              Solve by row equivalent or inverse matrix method:
29.
              x + z = 1
              z + 2v = 2.
              5x - 9y = -3
                                                                                              [Q.N.10 (b), 2066]
30. Solve by matrix inversion method: x + y = 3 and x - y = 1.
              (Ans: 2, 1)
                                                                                                             2 [Q.N. 3 (b), 2067]
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31.
        Solve by Cramer's rule or Row-equivalent method:
        x + y + z = 9, 2x + 5y + 7z = 52, 2x + y - z = 0
                                                                       4 [Q.N.10 (b), 2067]
        (Ans: 1, 3, 5)
32.
        Using Cramer's rule, solve the system of equations:
        2x + 5y = 17
        5x - 2y = -1
                                                                           [Q.N.3(a),2068]
        (Ans: x = 1, y = 3)
33.
        Applying row equivalent matrix method or inverse matrix method, solve the
        following system of equations:
        X + y + Z = 1
        x + 2y + 3z = 4
        x + 3y + 7z = 13
                                                                           [Q.N.8(a),2068]
        (Ans: x = 1, y = -3, z = 3)
        Using Cramer's rule, solve the following equations: I a swickled a later
34.
                x - 2y = -7
                 3x + 7y = 5
                                                                   [Q.N. 3(a), Set 'A' 2069]
        [Ans: -3, 2]
35.
        Using row equivalent matrix method or
                                                      inverse matrix method, solve the
        following equations.
                x - 2y - z = -7
                 2x + y + z = 0
                 3x - 5y + 8z = 13
        (Ans: -2, 1, 3) [Q.N. 8(a), Set 'A' 2069]
Solve by Cramer's rule: 3x + 2y + 9 = 0, 2x - 3y + 6 = 0 [Q.N. 3(a), Set 'B' 2069]
36.
        (Ans: -3, 0)
        Using raw equivalent or inverse matrix method, solve the following system of
37.
        equations.
 x - y = 0, 2x - y + 4z = 18, -3x + z + 2 = 0
                                                                [Q.N. 8(a), Set 'B' 20691
        (Ans: 2, 2, 4)
38.
        Using Cramer's rule, solve the following equations.
        2x - 5y = 24
        2x + 3y = 12
                                                          [Q.N. 3(a), Supp. 2069]
        (Ans: 8.25, -1.5)
39.
        Using row equivalent matrix method or inverse matrix method, solve the
        following system.
        3x + 5y = 2
        2x - 3z = -7
        4y + 2z = 2
                                                   [Q.N. 8(a), Supp. 2069]
        (Ans: 4, -2, 5)
                                                                     (Ans: 2 loos 16
40.
        Using Cramer's rule, solve the following equations:
        3x - 2y = 8, 5x + 3y = 7. after the order of the means of
                                                                       [Q.N. 3(a), 2070 'C']
        (Ans: x = 2, y = -1)
41.
        Using row equivalent matrix method or inverse matrix method, solve the
        following equations.
        x + 4y + z = 18, 3x + 3y - 2z = 2, -4y + z = -7
                                                                       [Q.N. 8(a), 2070 'C']
        (Ans: x = 1, y = 3, z = 5)
42.
        Applying Cramer's rule, solve the following equations:
        3x + \frac{4}{v} = 10, -2x + \frac{3}{v} = -1.
                                                                       [Q.N. 3(a), 2070 'D']
        (Ans: 2, 1)
43.
        Using row equivalent matrix method or inverse matrix method, solve the
        following equations.

9y - 5x = 3, x + z = 1, z + 2y = 2
                                                                       [Q.N. 8(a), 2070 'D']
        (Áns: 3, 2, -2)
Solve by Inverse matrix method:
        2x + y = 7, x + 3y = 11.
                                                                       [Q.N. 3(a), 2071 'C']
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(Ans: x = 2, y = 3)
Using Cramer's rule or row-equivalent method solve the following system: x + y + z = 6, 2x + 3y + 5z = 23, 7x + 5y - 2z = 11[Q.N. 8(a), 2071 'C']
(Ans: x = 1, y = 2, z = 3)

- 46. Solve by Inverse matrix method: 5x - 3y = 9; 2x + 5y = 16 (Ans: x = 3, y = 2)

 [Q.N. 3(a), 2071 'D']
- 47. Using Cramer's rule or row-equivalent matrix method solve the following system: [Q.N. 8(a), 2071 'D'] x+y+z=6, x-y+z=2, 5x-9y=-3 [Ans: x=3, y=2, z=1]

Unit 8 - Complex Number

1. If
$$z = 3 + 4i$$
 and $w = 2 + i$, find $|zw|$ and $\left|\frac{z}{w}\right|$. [Q.N.4(a), 2056]

(Ans: $5\sqrt{5}$ and $\sqrt{5}$)

State De- Moivre's theorem. Use it to find the cube roots of unity.

[Q.N.11(a), 2056]

(Ans: 1,
$$\frac{-1+i\sqrt{3}}{2}$$
 and $\frac{-1-i\sqrt{3}}{2}$)

3. If $Z_1 = (3, 2)$; $Z_2 = (5, 3)$, compute $Z_1 Z_2$ and $Z_1 + Z_2$ [Q.N.4(b), 2057]

(Ans:
$$Z_1Z_2 = (9, 19)$$
 and $Z_1 + Z_2 = (8, -5)$)

- 4. State De-Moivre's Theorem. Use it to find the values of $(1+i)^{20}$ [Q.N.11(b), 2057] (Ans: -2^{10})
- Express the complex number (2, 2√3) in the polar form. [Q.N.4(a), 2058]
 (Ans: 4 [cos60° + i sin 60°])
- 6. State De-Moivre's theorem. Use it to find the cube roots of 1. [Q.N.11(a), 2058] $1 1 + i\sqrt{3} 1 i\sqrt{3}$
 - (Ans: 1, $\frac{-1+i\sqrt{3}}{2}$ & $\frac{-1-i\sqrt{3}}{2}$) Express in the polar form for z = 2 + 2i.

7.

(Ans: $2\sqrt{2}$ (cos45° + / sin45°)) 8. Find the square roots of z = 7 - 24i. [Q.N.11(a), 2059]

[Q.N.4(a), 2059]

- 6. Find the square roots of Z = 7 24i.

 (Ans: ± (4 3i))
- 9. Express the complex number, $-\sqrt{2} + i\sqrt{2}$ in polar form. [Q.N.4(a), 2060] (Ans: 2 (cos 135° + *i* sin 135°))
- 10. Using De Moiver's theorem, find the fourth roots of unity. [Q.N.11(a), 2060] (Ans: 1, i, -1, -i)
- 11. Find the conjugate of the complex number $\frac{3+4i}{3-4i}$ [Q.N.4(a), 2061] $\left(\text{Ans: } Z = \overline{Z} = \frac{-7}{25} \frac{24}{25}i\right)$
- 12. State De Moivre's theorem hence solve $z^6 = 1$. [Q.N.11(a), 2061] $\left(\text{Ans: } \pm 1, \pm \left(\frac{1}{2} + i\frac{\sqrt{3}}{2}\right), \pm \left(\frac{1}{2} i\frac{\sqrt{3}}{2}\right)\right)$
- 13. Simplify: $[3 (\cos \frac{\pi}{4} + i \sin \frac{\pi}{4})]^{16}$ [Q.N.4(a), 2062]
- 14. Find the cube roots of unity. Write their properties. [Q.N.11(a), 2062] $\left(\text{Ans: } 1, \frac{-1+i\sqrt{3}}{2} \text{ and } \frac{-1-i\sqrt{3}}{2}\right)$